

MTH-4106 Factoring and Algebraic Fractions: **Worksheet #5**Factor the following trinomials using the **product-sum method (4 step method)**:

1.  $3x^2 + 14x + 8$

$P = 24$

$S = 14$

$2, 12$

$$(3x^2 + 2x) + (12x + 8)$$

$$\times (3x + 2) + 4(3x + 2)$$

$$(x + 4)(3x + 2)$$

2.  $7y^2 - 19y - 6$

$P = -42$

$S = -19$

$-21, +2$

$$(7y^2 - 21y) + (2y - 6)$$

$$7y(y - 3) + 2(y - 3)$$

$$(7y + 2)(y - 3)$$

3.  $3a^2 + a - 2$

$P = -6$

$S = +1$

$+3, -2$

$$(3a^2 + 3a) + (-2a - 2)$$

$$3a(a + 1) - 2(a + 1)$$

$$(3a - 2)(a + 1)$$

4.  $2x^2 - x - 1$

$P = -2$

$S = -1$

$-2, +1$

$$(2x^2 - 2x) + (1x - 1)$$

$$2x(x - 1) + 1(x - 1)$$

$$(2x + 1)(x - 1)$$

5.  $3p^2 + 10pq + 7q^2$

$P = 21$

$S = 10$

$3, 7$

$$(3p^2 + 3pq) + (7pq + 7q^2)$$

$$3p(p + q) + 7q(p + q)$$

$$(3p + 7q)(p + q)$$

6.  $15 - 2b - b^2$

$P = -15$

$S = -2$

$-5, 3$

$$(-b^2 - 5b) + (3b + 15)$$

$$-b(b + 5) + 3(b + 5)$$

$$(-b + 3)(b + 5)$$

7.  $3j^2 + 8jk + 4k^2$

$$P = 12$$

$$S = 8$$

$$2, 6$$

$$\begin{aligned} & (3j^2 + 2jk) + (6jk + 4k^2) \\ & j(3j + 2k) + 2k(3j + 2k) \\ & \boxed{(j+2k)(3j+2k)} \end{aligned}$$

8.  $3x^2 + 41xy + 26y^2$

$$P = 78$$

$$S = 41$$

$$2, 39$$

$$\begin{aligned} & (3x^2 + 2xy) + (39xy + 26y^2) \\ & x(3x + 2y) + 13y(3x + 2y) \\ & \boxed{(x+13y)(3x+2y)} \end{aligned}$$

9.  $-3x^2 + 10xy - 3y^2$

$$P = +9$$

$$S = 10$$

$$9, 1$$

$$\begin{aligned} & (-3x^2 + 9xy) + (10xy - 3y^2) \\ & -3x(x - 3y) + y(x - 3y) \\ & \boxed{(-3x+y)(x-3y)} \end{aligned}$$

10.  $3a^2 - 10ab + 3b^2$

$$P = 9$$

$$S = -10$$

$$-9, -1$$

$$\begin{aligned} & (3a^2 - 9ab) + (10ab + 3b^2) \\ & 3a(a - 3b) - b(a - 3b) \\ & \boxed{(3a-b)(a-3b)} \end{aligned}$$

11.  $-b^2 - b + 20$

$$P = -20$$

$$S = -1$$

$$-5, +4$$

$$\begin{aligned} & (-b^2 - 5b) + (4b + 20) \\ & -b(b + 5) + 4(b + 5) \\ & \boxed{(-b+4)(b+5)} \end{aligned}$$

12.  $2x^2 - 7xy + 5y^2$

$$P = 10$$

$$S = -7$$

$$-2, -5$$

$$\begin{aligned} & (2x^2 - 2xy) + (5xy + 5y^2) \\ & 2x(x - y) - 5y(x - y) \\ & \boxed{(2x-5y)(x-y)} \end{aligned}$$

13.  $8a^2 - 14ab + 3b^2$

$P = 24$

$S = -14$

-2, -12

$$\frac{(8a^2 - 2ab)(-12ab + 3b^2)}{2a(4a-b) - 3b(4a-b)}$$

$$\boxed{(2a-3b)(4a-b)}$$

14.  $5a^2 - 26ab + 5b^2$

$P = 25$

$S = -26$

-25, -1

$$\frac{(5a^2 - 25ab)(-1ab + 5b^2)}{5a(a-5b) - b(a-5b)}$$

$$\boxed{(5a-b)(a-5b)}$$

15.  $9y^2 - 6y + 1$

$P = 9$

$S = -6$

-3, -3

$$\frac{(9y^2 - 3y)(-3y + 1)}{3y(3y-1) - 1(3y-1)}$$

$$\boxed{(3y-1)(3y-1)}$$

16.  $3x^2 - 13x + 4$

$P = 12$

$S = -13$

-12, -1

$$\frac{(3x^2 - 12x)(-1x + 4)}{3x(x-4) - 1(x-4)}$$

$$\boxed{(3x-1)(x-4)}$$

17.  $6t^2 - 19t + 3$

$P = 18$

$S = -19$

-18, -1

$$\frac{(6t^2 - 18t)(-1t + 3)}{6t(t-3) - 1(t-3)}$$

$$\boxed{(6t-1)(t-3)}$$

18.  $15a^2 - 13ab + 2b^2$

$P = 30$

$S = -13$

-3, -10

$$\frac{(15a^2 - 3ab)(-10ab + 2b^2)}{3a(5a-b) - 2b(5a-b)}$$

$$\boxed{(3a-2b)(5a-b)}$$

19.  $4x^2 - 17xy + 4y^2$

$$\begin{aligned} p &= 16 \\ s &= -17 \\ &-16, -1 \end{aligned}$$

$$\begin{aligned} &(4x^2 - 16xy) - 1xy + 4y^2 \\ &4x(x - 4y) - y(x - 4y) \\ &\boxed{(4x - y)(x - 4y)} \end{aligned}$$

20.  $-b^2 - b + 6$

$$\begin{aligned} p &= -6 \\ s &= -1 \\ &-3, +2 \end{aligned}$$

$$\begin{aligned} &(-b^2 - 3b) + (2b + 6) \\ &-b(b + 3) + 2(b + 3) \\ &\boxed{(-b + 2)(b + 3)} \end{aligned}$$

21.  $2x^2 - 5xy + 2y^2$

$$\begin{aligned} p &= 4 \\ s &= -5 \\ &-4, -1 \end{aligned}$$

$$\begin{aligned} &(2x^2 - 4xy) - 1xy + 2y^2 \\ &2x(x - 2y) - y(x - 2y) \\ &\boxed{(2x - y)(x - 2y)} \end{aligned}$$

22.  $3x^2 - 7x + 2$

$$\begin{aligned} p &= 6 \\ s &= -7 \\ &-6, -1 \end{aligned}$$

$$\begin{aligned} &(3x^2 - 6x) + 1x + 2 \\ &3x(x - 2) - 1(x - 2) \\ &\boxed{(3x - 1)(x - 2)} \end{aligned}$$

23.  $-2x^2 + 13x - 15$

$$\begin{aligned} p &= 30 \\ s &= 13 \\ &3, 10 \end{aligned}$$

$$\begin{aligned} &(-2x^2 + 3x) + (10x - 15) \\ &-x(2x - 3) + 5(2x - 3) \\ &\boxed{(-x + 5)(2x - 3)} \end{aligned}$$

24.  $-4y^2 + 9xy - 2x^2$

$$\begin{aligned} p &= 8 \\ s &= 9 \\ &8, 1 \end{aligned}$$

$$\begin{aligned} &(-4y^2 + 8xy) + 1xy - 2x^2 \\ &-4y(y - 2x) + x(y - 2x) \\ &\boxed{(-4y + x)(y - 2x)} \end{aligned}$$

25.  $2b^2 + 5b + 2$   $(2b^2 + 4b) + (1b + 2)$

$$P = 4$$

$$S = 5$$

$$4, 1$$

$$\frac{2b(b+2) + 1(b+2)}{(2b+1)(b+2)}$$

26.  $2x^2 + 7x + 3$   $(2x^2 + 6x) + (1x + 3)$

$$P = 6$$

$$S = 7$$

$$6, 1$$

$$\frac{2x(x+3) + 1(x+3)}{(2x+1)(x+3)}$$

27.  $2a^2 + 9a + 4$   $(2a^2 + 8a) + (1a + 4)$

$$P = 8$$

$$S = 9$$

$$8, 1$$

$$\frac{2a(a+4) + 1(a+4)}{(2a+1)(a+4)}$$

28.  $2 + 9x - 18x^2$   $(-18x^2 + 12x) + (3x + 2)$

$$-18x^2 + 9x + 2$$

$$P = -36$$

$$S = +9$$

$$12, -3$$

$$-6x(3x-2) + 1(3x-2)$$

$$\frac{(-6x+1)(3x-2)}{(-6x-1)(3x-2)}$$

29.  $-12x^2 - xy + y^2$   $(-12x^2 - 4xy) + (3xy + y^2)$

$$P = -12$$

$$S = -1$$

$$-4, +3$$

$$\frac{-4x(3x+y) + y(3x+y)}{(-4x+y)(3x+y)}$$

30.  $2x^2 + 9x + 9$   $(2x^2 + 3x) + (6x + 9)$

$$P = 18$$

$$S = 9$$

$$3, 6$$

$$x(2x+3) + 3(2x+3)$$

$$\boxed{x+3)(2x+3)}$$

31.  $4y^2 - 4y + 1$   
 $p = 4$   
 $s = -4$   
 $-2, -2$

$$\frac{(4y^2 - 2y)(2y + 1)}{2y(2y - 1) - 1(2y - 1)}$$

$$\boxed{(2y - 1)(2y + 1)}$$

32.  $-7x^2 - 13xy + 2y^2$   
 $p = -14$   
 $s = -13$   
 $-14, +1$

$$\frac{(-7x^2 - 14xy)(1xy + 2y^2)}{-7x(x + 2y) + y(x + 2y)}$$

$$\boxed{(-7x + y)(x + 2y)}$$

33.  $1 - 3m + 2m^2$   
 $p = 2$   
 $s = -3$   
 $-2, -1$

$$\frac{(2m^2 - 2m)(-1m + 1)}{2m(m - 1) - 1(m - 1)}$$

$$\boxed{(2m - 1)(m - 1)}$$

34.  $-6x^2 + xy + 2y^2$   
 $p = -12$   
 $s = +1$   
 $+4, -3$

$$\frac{(-6x^2 + 4xy)(-3xy + 2y^2)}{-2x(3x - 2y) - y(3x - 2y)}$$

$$\boxed{(-2x - y)(3x - 2y)}$$

35.  $6 - 7t + 2t^2$   
 $p = 12$   
 $s = -7$   
 $-3, -4$

$$\frac{(2t^2 - 3t)(-4t + 6)}{t(2t - 3) - 2(2t - 3)}$$

$$\boxed{(t - 2)(2t - 3)}$$

36.  $19a + 5 - 4a^2$   
 $-4a^2 + 19a + 5$   
 $p = -20$   
 $s = 19$   
 $20, -1$

$$\frac{(-4a^2 + 20a)(-1a + 5)}{4a(-a + 5) + 1(-a + 5)}$$

$$\boxed{(4a + 1)(-a + 5)}$$

37.  $10x^2 - x - 2$

$$P = -20$$

$$S = -1$$

$$-5, +4$$

$$\frac{(10x^2 - 5x) + (4x - 2)}{5x(2x - 1) + 2(2x - 1)}$$

$$\boxed{(5x+2)(2x-1)}$$

38.  $-8a^2 + 6ab - b^2$

$$P = 8$$

$$S = 6$$

$$2, 4$$

$$\frac{(-8a^2 + 2ab) + (4ab - b^2)}{2a(-4a + b) - b(-4a + b)}$$

$$\boxed{(2a-b)(-4a+b)}$$

39.  $-x^2 - 2x - 1$

$$P = 1$$

$$S = -2$$

$$-1, -1$$

$$\frac{(-x^2 - 1x) - (-1x - 1)}{-x(x+1) - 1(x+1)}$$

$$\boxed{(-x-1)(x+1)}$$

40.  $1 - 16y + 64y^2$

$$P = 64$$

$$S = -16$$

$$-8, -8$$

$$\frac{(64y^2 - 8y) - (8y + 1)}{8y(8y - 1) - 1(8y - 1)}$$

$$\boxed{(8y-1)(8y+1)}$$

41.  $5j^2 - 6j - 8$

$$P = -40$$

$$S = -6$$

$$-10, +4$$

$$\frac{(5j^2 - 10j) + (4j - 8)}{5j(j - 2) + 4(j - 2)}$$

$$\boxed{(5j+4)(j-2)}$$

42.  $12c^2 - 23cd + 10d^2$

$$P = 120$$

$$S = -23$$

$$-8, -15$$

$$\frac{(12c^2 - 8cd) - (15cd + 10d^2)}{4c(3c - 2d) - 5d(3c - 2d)}$$

$$\boxed{(4c-5d)(3c-2d)}$$