

MTH-4106 Factoring and Algebraic Fractions: **Worksheet #8**

Factor the following polynomials **completely**:

e.g. 1 $3x^2 + 6x - 9$

e.g. 2 $3x^3 - 9x^2 - 12x$

e.g. 3 $2p^2 - 4pq - 48q^2$

e.g. 4 $8y^4 - 2y^3z - 6y^2z^2$

e.g. 5 $27ax^2 - 48ay^2$

e.g. 6 $16a^4 - 81b^4$

e.g. 7 $2abc^2 + 6abc - 8abc - 24ab$

Now you do:

1. $3ax - 3ax^3$

2. $6x^3y - 72x^2 - 18x^2y + 24x^3$

3. $-4x^2y^4 + 2x^3y^3 + 12x^4y^2$

4. $24x^2 + 12x + 8xy + 4y$

5. $3d^2e^6 - 48d^2f^8$

$$6. \quad 12a^4 + 32a^3 - 12a^2$$

$$7. \quad 45x^4y^3 - 39x^3y^4 + 6x^2y^5$$

$$8. \quad 16x^4y^2 - 68x^3y^3 + 16x^2y^4$$

$$9. \quad 9a^2 - 36y^4$$

$$10. \quad 4 - 4b^2$$

$$11. \quad 2y^3 + 6y + 2y^2 + 6$$

12. $6b^2 - 21b - 45$

13. $3x^2 + 6xy + 3y^2$

14. $5x^2 - 5y^2$

15. $5x^2 + 35xy + 30y^2$

16. $50 - 2a^2$

17. $5x^2 + 30x - 35$

$$18. \quad 3x^5y^3 + x^4y^4 - 2x^3y^5$$

$$19. \quad b^2y^2 - 4b^2$$

$$20. \quad 27a^2b^2 - 12a^4$$

$$21. \quad -3x^3y + 10x^2y^2 - 3xy^3$$

$$22. \quad 4m^3 - 9m^2 + 2m$$

$$23. \quad -3x^3 - 8x^2 + 3x$$

$$24. \quad 12x^2 + 4xy + 6x + 2y$$

$$25. \quad 2p^5q^2 - p^4q^3 - p^3q^4$$

$$26. \quad 4a^4b + a^3b^2 - 3a^2b^3$$

$$27. \quad 3x^8z^3 - 75y^6z^3$$

$$28. \quad 18m^8n^2 - 2p^2n^2$$

$$29. \quad -18a^2x^3 + 15a^2x^2y - 3a^2xy^2$$

$$30. \quad 3a^2 - 9ab + 6b^2$$

$$31. \quad 32 - 2c^2$$

$$32. \quad -2g^4h + 20g^3h^2 - 48g^2h^3$$

$$33. \quad 7x^4 - 28$$

$$34. \quad 12x^3 + 144x + 84x^2$$

$$35. \quad 10rs - 5rt + 20s^2 - 10st$$

$$36. \quad c^3 - 36a^4b^2c$$

$$37. \quad 2a^4 - 20a^3b + 50a^2b^2$$

$$38. \quad -a^5 + 13a^4 - 42a^3$$

$$39. \quad 3 - 3t^2$$

$$40. \quad 2uvx - 4uvy - 4ux + 8uy$$

Answers to Worksheet #8

1. $3ax(1-x)(1+x)$
2. $6x^2(y+4)(x-3)$
3. $2x^2y^2(2y+3x)(-y+2x)$
4. $4(3x+y)(2x+1)$
5. $3d^2(e^3-4f^4)(e^3+4f^4)$
6. $4a^2(3a-1)(a+3)$
7. $3x^2y^3(3x-2y)(5x-y)$
8. $4x^2y^2(4x-y)(x-4y)$
9. $9(a-2y^2)(a+2y^2)$
10. $4(1-b)(1+b)$
11. $2(y^2+3)(y+1)$
12. $3(b-5)(2b+3)$
13. $3(x+y)^2$
14. $5(x+y)(x-y)$
15. $5(x+6y)(x+y)$
16. $2(5-a)(5+a)$
17. $5(x+7)(x-1)$
18. $x^3y^3(3x-2y)(x+y)$
19. $b^2(y-2)(y+2)$
20. $3a^2(3b+2a)(3b-2a)$
21. $xy(-3x+y)(x-3y)$
22. $m(4m-1)(m-2)$
23. $x(-3x+1)(x+3)$
24. $2(3x+y)(1+2x)$
25. $p^3q^2(2p+q)(p-q)$
26. $a^2b(4a-3b)(a+b)$
27. $3z^3(x^4-5y^3)(x^4+5y^3)$
28. $2n^2(3m^4-p)(3m^4+p)$
29. $3a^2x(-2x+y)(3x-y)$
30. $3(a-2b)(a-b)$
31. $2(4-c)(4+c)$
32. $2g^2h(-g+6h)(g-4h)$
33. $7(x^2-2)(x^2+2)$
34. $12(x+3)(x+4)$
35. $5(c+2s)(2s-t)$
36. $c(c-6a^2b)(c+6a^2b)$
37. $2a^2(a-5b)(a-5b)$
38. $\ell^3(-a+7)(a-6)$
39. $3(1-t)(1+t)$
40. $2v(v-2)(x-2y)$